

$(a+b+c)^2$ を展開しなさい #20 その 3 例 2

数学が苦手な人はコツコツ計算しよう…

$(a+b+c)^2$ を展開しなさい #20 その 3 例 2

数学が苦手な人はコツコツ計算しよう…

$$\begin{aligned} & (a+b+c)^2 \\ = & (a+b+c)(a+b+c) \end{aligned}$$

$(a+b+c)^2$ を展開しなさい #20 その 3 例 2

数学が苦手な人はコツコツ計算しよう…

$$\begin{aligned} & (a+b+c)^2 \\ = & (a+b+c)(a+b+c) \\ = & a \cdot a + a \cdot b + a \cdot c + b \cdot a + b \cdot b + b \cdot c + c \cdot a + c \cdot b + c \cdot c \\ = & a^2 + ab + ac + ba + b^2 + bc + ca + cb + c^2 \\ = & a^2 + ab + ca + ab + b^2 + bc + ca + bc + c^2 \\ = & a^2 + b^2 + c^2 + 2ab + 2bc + 2ca \quad \boxed{\text{答}} \end{aligned}$$

置き換えると少しだけ楽になるかも…

置き換えると少しだけ楽になるかも…

$a + b = A$ とおくと

$$\begin{aligned} & (a + b + 2)^2 \\ = & (A + c)^2 \end{aligned}$$

置き換えると少しだけ楽になるかも…

$$a + b = A \text{ とおくと}$$

$$(a + b + 2)^2$$

$$= (A + c)^2$$

$$= A^2 + 2Ac + c^2$$

置き換えると少しだけ楽になるかも…

$$a+b = A \text{ とおくと}$$

$$(a+b+2)^2$$

$$= (A+c)^2$$

$$= A^2 + 2Ac + c^2 \quad \text{元に戻す}$$

$$= (a+b)^2 + 2(a+b)c + c^2$$

置き換えると少しだけ楽になるかも…

$$a+b = A \text{ とおくと}$$

$$(a+b+2)^2$$

$$= (A+c)^2$$

$$= A^2 + 2Ac + c^2 \quad \text{元に戻す}$$

$$= (a+b)^2 + 2(a+b)c + c^2$$

$$= a^2 + 2ab + b^2 + 2ac + 2bc + c^2 \quad \boxed{\text{答}}$$

余力がある人は暗記すればよいが...

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$$

無理な人はあきらめま
しょう

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

例題

$$(a + 3b + 2)^2$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

例題

$$(a + 3b + 2)^2$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

例題

$$\begin{aligned} & (a + 3b + 2)^2 \\ &= \underbrace{a^2 + (3b)^2 + 2^2}_{2 \text{ 乗}} + \underbrace{2a \cdot 3b + 2 \cdot 3b \cdot 2 + 2 \cdot 2 \cdot a}_{2 \times \text{ かけ算}} \end{aligned}$$

こうすれば少しはマシ？

$$\begin{aligned} & (a + 3b + 2)^2 \\ &= \underbrace{a^2 + (3b)^2 + 2^2}_{2 \text{ 乗}} + \underbrace{2a \cdot 3b + 2 \cdot 3b \cdot 2 + 2 \cdot 2 \cdot a}_{2 \times \text{かけ算}} \\ &= a^2 + 9b^2 + 4 + 6ab + 12b + 4a \quad \boxed{\text{答}} \end{aligned}$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

例題

$$(a + 2b - 1)^2$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

例題

$$\begin{aligned} & (a + 2b - 1)^2 \\ &= \left(a + 2b + (-1) \right)^2 \end{aligned}$$

こうすれば少しはマシ？

$$\begin{aligned} & (\text{●} + \text{▲} + \text{■})^2 \\ &= \underbrace{\text{●}^2 + \text{▲}^2 + \text{■}^2}_{2 \text{ 乗}} + \underbrace{2 \text{ ●▲} + 2 \text{ ▲■} + 2 \text{ ■●}}_{2 \times \text{ かけ算}} \end{aligned}$$

例題

$$\begin{aligned} & (a + 2b - 1)^2 \\ &= (a + 2b + (-1))^2 \\ &= \underbrace{a^2 + (2b)^2 + (-1)^2}_{2 \text{ 乗}} + \underbrace{2a \cdot 2b + 2 \cdot 2b \cdot (-1) + 2 \cdot (-1) \cdot a}_{2 \times \text{ かけ算}} \end{aligned}$$

こうすれば少しはマシ？

$$\begin{aligned}(a+2b-1)^2 &= (a+2b+(-1))^2 \\ &= a^2 + (2b)^2 + (-1)^2 + 2a \cdot 2b + 2 \cdot 2b \cdot (-1) + 2 \cdot (-1) \cdot a \\ &= a^2 + 4b^2 + 1 + 4ab - 4b - 2a \quad \boxed{\text{答}}\end{aligned}$$